

# Package ‘ZEP’

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**Type** Package

**Title** Procedures Related to the Zadeh's Extension Principle for Fuzzy Data

**Version** 0.1.3

**Description** Procedures for calculation, plotting, and approximation of the outputs for fuzzy numbers (see A.I. Ban, L. Coroianu, P. Grzegorzewski ``Fuzzy Numbers: Approximations, Ranking and Applications" (2015)) based on the Zadeh's Extension Principle (see de Barros, L.C., Bassanezi, R.C., Lodwick, W.A. (2017) <[doi:10.1007/978-3-662-53324-6\\_2](https://doi.org/10.1007/978-3-662-53324-6_2)>).

**License** GPL-3

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**Depends** R (>= 3.5.0)

**Suggests** testthat (>= 3.0.0)

**Config/testthat/edition** 3

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ApplyZFunction	<i>Function to apply the Zadeh’s principle</i>
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Description

ApplyZFunction applies the selected function to a fuzzy number using the Zadeh’s principle.

Usage

```
ApplyZFunction(  
  value,  
  FUN,  
  knots = 10,  
  approximation = FALSE,  
  method = "NearestEuclidean",  
  ...  
)
```

Arguments

value	Input fuzzy number.
FUN	Function used for the input fuzzy number with the help of the Zadeh’s principle.
knots	Number of the alpha-cuts used during calculation of the output.
approximation	If TRUE, the approximated output is calculated.
method	The selected approximation method.
...	Additional parameters passed to other functions.

Details

The function takes the input fuzzy number value (which should be described by one of the classes from FuzzyNumbers package) and applies the function FUN using the Zadeh’s principle. The output is given by a fuzzy number or its approximation (when approximation is set to TRUE and the respective method is selected). To properly find the output, value of FUN is calculated for many alpha-cuts of value. The number of these alpha-cuts is equal to knots (plus 2 for the support and the core).

The input fuzzy number value should be given by fuzzy number described by classes from FuzzyNumbers package.

**Value**

The output is a fuzzy number described by classes from FuzzyNumbers package (piecewise linear fuzzy number without approximation, various types with the approximation applied).

**Examples**

```
library(FuzzyNumbers)

# prepare complex fuzzy number

A <- FuzzyNumber(-5, 3, 6, 20, left=function(x)
  pbeta(x,0.4,3),
  right=function(x) 1-x^(1/4),
  lower=function(alpha) qbeta(alpha,0.4,3),
  upper=function(alpha) (1-alpha)^4)

# find the output via the Zadeh's principle

ApplyZFunction(A,FUN=function(x)x^3+2*x^2-1)

# find the approximated output via the Zadeh's principle

ApplyZFunction(A,FUN=function(x)x^3+2*x^2-1,approximation=TRUE)
```

---

```
approximationMehodsInside
```

*A vector containing names of the built-in approximation methods.*

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**Description**

‘approximationMehodsInside’ is a vector containing names of the built-in approximation methods.

**Usage**

```
approximationMehodsInside
```

**Format**

An object of class character of length 2.

**Value**

This function returns a vector of strings.

**Examples**

```
# check the names
approximationMehodsInside
```

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DpqDistance

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*Function to calculate  $D(p,q)$  distance.*


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**Description**

DpqDistance calculates the generalized  $D(p,q)$  distance between two fuzzy numbers.

**Usage**

```
DpqDistance(value1, value2, p = 2, q = 1/2)
```

**Arguments**

value1	First fuzzy number.
value2	Second fuzzy number.
p	Value of the power (and the the root) applied in the distance calculation.
q	Value of the weight for the second fuzzy number (for the first one this weight is calculated as $1-q$ , respectively).

**Details**

The function calculates the generalized  $D(p,q)$  distance between two fuzzy numbers value1 and value2, where p is the value of the applied power, and q is the weight between these two fuzzy numbers.

All of the input values should be given by fuzzy numbers described by classes from FuzzyNumbers package.

**Value**

The output is a numerical value (the calculated distance).

**Examples**

```
library(FuzzyNumbers)

# prepare two fuzzy numbers

A <- TrapezoidalFuzzyNumber(0,1,2,3)

B <- TrapezoidalFuzzyNumber(1,3,4,6)
```

```
# calculate the distance

DpqDistance (A,B)
```

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FuzzyApproximation	<i>Function for approximation with the help of methods other than in FuzzyNumbers package</i>
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## Description

FuzzyApproximation approximates the given fuzzy number.

## Usage

```
FuzzyApproximation(value, method = "ExpectedValueCore", ...)
```

## Arguments

value	Fuzzy number to approximate.
method	The selected approximation method.
...	Additional parameters passed to other functions.

## Details

The function approximates the fuzzy number given by value with the method selected by method. The following approximations are possible: ExpectedValueCore—preserving the expected value and the core of value, TriangularSupportDist—constructs the triangular fuzzy number based on minimization of DpqDistance, preserving the support of value.

The input value should be given by a fuzzy number described by classes from FuzzyNumbers package.

## Value

The output is a fuzzy number (triangular or trapezoidal one) described by classes from FuzzyNumbers package.

## Examples

```
library(FuzzyNumbers)

# prepare complex fuzzy number

A <- FuzzyNumber(-5, 3, 6, 20, left=function(x)
pbeta(x,0.4,3),
right=function(x) 1-x^(1/4),
```

```

lower=function(alpha) qbeta(alpha,0.4,3),
upper=function(alpha) (1-alpha)^4)

# find approximation

FuzzyApproximation (A)

```

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PlotZFunction

*Plot input and output for the Zadeh's principle*


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## Description

PlotZFunction applies the selected function to a fuzzy number using the Zadeh's principle, and plots the input and output.

## Usage

```

PlotZFunction(
  value,
  FUN,
  knots = 10,
  grid = TRUE,
  alternate = FALSE,
  approximation = FALSE,
  method = "NearestEuclidean",
  ...
)

```

## Arguments

value	Input fuzzy number.
FUN	Function used for the input fuzzy number with the help of the Zadeh's principle.
knots	Number of the alpha-cuts used during calculation of the output.
grid	If TRUE, then additional grid is plotted.
alternate	If TRUE, the second type of the layout of figures is used.
approximation	If TRUE, the approximated output is calculated.
method	The selected approximation method.
...	Additional parameters passed to other functions.

## Details

The function takes the input fuzzy number value (which should be described by one of the classes from FuzzyNumbers package) and applies the function FUN using the Zadeh's principle. The output is given by a fuzzy number or its approximation (when approximation is set to TRUE and the respective method is selected). To properly find the output, value of FUN is calculated for many alpha-cuts of value. The number of these alpha-cuts is equal to knots (plus 2 for the support and the core). The input and output fuzzy numbers are plotted together with the applied function. If the approximation is used, then also the approximated fuzzy number is shown (green line).

The input fuzzy number value should be given by fuzzy number described by classes from FuzzyNumbers package.

## Value

Three (or four) figures are plotted: the input fuzzy number, the respective output (for the Zadeh's principle and the applied function), and the function. The output fuzzy number can be approximated with the selected method and also plotted.

## Examples

```
library(FuzzyNumbers)

# prepare complex fuzzy number

A <- FuzzyNumber(-5, 3, 6, 20, left=function(x)
pbeta(x,0.4,3),
right=function(x) 1-x^(1/4),
lower=function(alpha) qbeta(alpha,0.4,3),
upper=function(alpha) (1-alpha)^4)

# plot the figures

PlotZFunction(A,FUN=function(x)x^3+2*x^2-1)

# find and plot the approximated output via the Zadeh's principle

PlotZFunction(A,FUN=function(x)x^3+2*x^2-1,approximation=TRUE)
```

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