# Package 'netcom'

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Type Package

Title NETwork COMparison Inference

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**Description** Infer system functioning with empirical NETwork COMparisons. These methods are part of a growing paradigm in network science that uses relative comparisons of networks to infer mechanistic classifications and predict systemic interventions. They have been developed and applied in Langendorf and Burgess (2021) <doi:10.1038/s41598-021-99251-7>, Langendorf (2020) <doi:10.1201/9781351190831-6>, and Langendorf and Goldberg (2019) <doi:10.48550/arXiv.1912.12551>.

URL https://github.com/langendorfr/netcom

Repository CRAN

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2 align

# **Contents**

align	Network Alignment		
Index			61
	stir_SW		59
	stir PA		58
	stir NM		56
	stir ER		55
	stir DM		54
	stir DD		53
	null_fit_optim		+c 50
	make_Systematic_mixture		40 48
	make_Systematic_canonical		44 46
	make_Systematic		42 44
	make_SW		41 42
	make_Null_mixture		38
	make_Null_canonical		36
	make_Null		33
	make_NM		32
	make_Mixture		30
	make_DM		29
	make_DD		28
	ics		27
	grow_SW		26
	grow_PA		24
	grow_NM	2	23
	grow_ER		22
	grow_DM	2	21
	grow_DD		19
	gini		19
	compare_Target		17
	compare		15
	classify_Systematic		12
	classify		8
	best_fit_optim		5
	align		2

# Description

Network alignment by comparing the entropies of diffusion kernels simulated on two networks. align takes two networks stored as matrices and returns a node-level alignment between them.

align 3

### Usage

```
align(
  network_1_input,
  network_2_input,
  base = 2,
  max_duration,
  characterization = "entropy",
  normalization = FALSE,
  unit_test = FALSE
)
```

#### Arguments

network\_1\_input

The first network being aligned, which must be in matrix form. If the two networks are of different sizes, it will be easier to interpret the output if this is the smaller one.

network\_2\_input

The second network, which also must be a matrix.

base

Defaults to 1. The base in the series of time steps to sample the diffusion kernels at. If base = 1 every time step is sampled. If base = 2, only time steps that are powers of 2 are sampled, etc. Larger values place more emphasis on earlier time steps. This can be helpful if the diffusion kernel quickly converges to an equilibrium, and also runs faster.

max\_duration

Defaults to twice the diameter of the larger network. Sets the number of time steps to allow the diffusion kernel to spread for, which is the smallest power of base that is at least as large as max\_duration.

characterization

Defaults to "entropy". Determines how the diffusion kernels are characterized. Either "entropy" or "gini". "entropy" is a size-normalized version of Shannon's entropy with base e (Euler's number). This is also known as interaction or species evenness in ecology. "gini" is the Gini coefficient.

normalization

Defaults to FALSE. Determines if self-loops should be augmented such that edge weights are proportional to those in network\_1\_input and network\_2\_input. FALSE by default because this is inappropriate for unweighted binary/logical networks where edges indicate only the presence of an interaction.

 $unit\_test$ 

Defaults to FALSE. Saves the following intermediate steps to help with general troubleshooting: post-processing matrix representations of both networks, time steps at which the diffusion kernels were sampled, the diffusion kernels at those time steps, the characterizations of the diffusion kernels at those time steps, and the cost matrix fed into the Hungarian algorithm where the ij element is the difference between the characterization-over-time curves for node i in the first network and node j in the second network.

### Details

Network alignment pairs nodes between two networks so as to maximize similarities in their edge structures. This allows information from well-studied systems to be used in poorly studied ones,

4 align

such as to identify unknown protein functions or ecosystems that will respond similarly to a given disturbance. Most network alignment algorithms focus on measures of topological overlap between edges of the two networks. The method implemented here compares nodes using the predictability of dynamics originating from each node in each network. Consider network alignment as trying to compare two hypothetical cities of houses connected by roads. The approach implemented here is to pairwise compare each house with those in the other city by creating a house-specific signature. This is accomplished by quantifying the predictability of the location of a person at various times after they left their house, assuming they were moving randomly. This predictability across all houses captures much of the way each city is organized and functions. align uses this conceptual rationale to align two networks, with nodes as houses, edges as roads, and random diffusion representing people leaving their houses and walking around the city to other houses. The mechanics of this, which are conceptually akin to flow algorithms and Laplacian dynamics, can be analytically expressed as a Markov chain raised to successive powers which are the durations of diffusion.

Note that the novel part of align lies in creating a matrix where the ij entry is a measure of similarity between node i in the first network and node j in the second. The final alignment is found using solve\_LSAP in the package clue, which uses the Hungarian algorithm to solve the assignment problem optimally.

#### Value

score Mean of all alignment scores between nodes in both original networks net-

work\_1\_input and network\_2\_input.

alignment Data frame of the nodes in both networks, sorted numerically by the first net-

work (why it helps to make the smaller network the first one), and the corre-

sponding alignment score.

score\_with\_padding

Same as score but includes the padding nodes in the smaller network, which can be thought of as a size gap penalty for aligning differently sized networks. Only

included if the input networks are different sizes.

alignment\_with\_padding

Same as alignment but includes the padding nodes in the smaller network. Only included if the input networks are different sizes.

### References

Kuhn, H. W. (1955). The Hungarian method for the assignment problem. Naval Research Logistics (NRL), 2(1-2), 83-97.

Langendorf, R. E., & Goldberg, D. S. (2019). Aligning statistical dynamics captures biological network functioning. arXiv preprint arXiv:1912.12551.

C. Papadimitriou and K. Steiglitz (1982), Combinatorial Optimization: Algorithms and Complexity. Englewood Cliffs: Prentice Hall.

```
# The two networks to be aligned
net_one <- matrix(stats::runif(25,0,1), nrow=5, ncol=5)
net_two <- matrix(stats::runif(25,0,1), nrow=5, ncol=5)</pre>
```

best\_fit\_optim 5

```
align(net_one, net_two)
align(net_one, net_two, base = 1, characterization = "gini", normalization = TRUE)
```

best\_fit\_optim

Empirical parameterization

### **Description**

Helper function to find the best fitting version of a mechanism by searching across its parameter space

# Usage

```
best_fit_optim(
  parameter,
  process,
  network,
  net_size,
  net_kind,
 mechanism_kind,
  resolution,
  resolution_min,
  resolution_max,
  reps,
  power_max,
  connectance_max,
  divergence_max,
 mutation_max,
  cores,
  directed,
  method,
  cause_orientation,
 DD_kind,
  DD_weight,
 max_norm,
 best_fit_kind = "avg",
  verbose = FALSE
)
```

# Arguments

parameter The parameter being tested for its ability to generate networks alike the input 'network'.

process Name of mechanism. Currently only "ER", "PA", "DD", "DM" "SW", and "NM" are supported. Future versions will accept user-defined network-generating

6 best\_fit\_optim

functions and associated parameters. ER = Erdos-Renyi random. PA = Preferential Attachment. DD = Duplication and Divergence. DM = Duplication and Mutation SW = Small World NM = Night Model

Mutation. SW = Small World. NM = Niche Model.

network The network being compared to a hypothesized 'process' with a given 'parame-

ter' value.

net\_size Number of nodes in the network.

net\_kind If the network is an adjacency matrix ("matrix") or an edge list ("list").

mechanism\_kind Either "canonical" or "grow" can be used to simulate networks. If "grow" is

used, note that here it will only simulate pure mixtures made of a single mecha-

nism.

resolution The first step is to find the version of each process most similar to the target

network. This parameter sets the number of parameter values to search across.

Decrease to improve performance, but at the cost of accuracy.

resolution\_min = The minimum parameter value to consider. Zero is not used because in many

processes it results in degenerate systems (e.g. entirely unconnected networks). Currently process agnostic. Future versions will accept a vector of values, one

for each process.

resolution\_max The maximum parameter value to consider. One is not used because in many

processes it results in degenerate systems (e.g. entirely connected networks). Currently process agnostic. Future versions will accept a vector of values, one

for each process.

reps The number of networks to simulate for each parameter. More replicates in-

creases accuracy by making the estimation of the parameter that produces net-

works most similar to the target network less idiosyncratic.

power\_max The maximum power of attachment in the Preferential Attachment process (PA).

connectance\_max

The maximum connectance parameter for the Niche Model.

divergence\_max The maximum divergence parameter for the Duplication and Divergence/Mutation

mechanisms.

mutation\_max The maximum mutation parameter for the Duplication and Mutation mecha-

nism.

cores The number of cores to run the classification on. When set to 1 parallelization

will be ignored.

directed Whether the target network is directed.

method This determines the method used to compare networks at the heart of the clas-

sification. Currently "DD" (Degree Distribution) and "align" (the align function which compares networks by the entropy of diffusion on them) are supported.

Future versions will allow user-defined methods.

cause\_orientation

The orientation of directed adjacency matrices.

DD\_kind A vector of network properties to be used to compare networks.

DD\_weight Weights of each network property in DD\_kind. Defaults to 1, which is equal

weighting for each property.

best\_fit\_optim 7

max\_norm
Binary variable indicating if each network property should be normalized so its max value (if a node-level property) is one.

best\_fit\_kind
How to aggregate the stochastic replicates of the process + parameter combination.

verbose
Defaults to TRUE. Whether to print all messages.

### **Details**

Note: Currently each process is assumed to have a single governing parameter.

#### Value

A number measuring how different the input network is from the parameter + process combination.

#### References

Langendorf, R. E., & Burgess, M. G. (2020). Empirically Classifying Network Mechanisms. arXiv preprint arXiv:2012.15863.

```
# Import netcom
library(netcom)
# Adjacency matrix
size <- 10
network <- matrix(sample(c(0,1), size = size^2, replace = TRUE), nrow = size, ncol = size)
# Calculate how similar the input network is to Small-World networks with
# a rewiring probability of 0.28.
best_fit_optim(
     parameter = 0.28,
     process = "SW",
    network = network,
    net_size = 12,
    net_kind = "matrix",
    mechanism_kind = "grow",
     resolution = 100,
     resolution_min = 0.01,
     resolution_max = 0.99,
     reps = 3,
    power_max = 5,
    connectance_max = 0.5,
     divergence_max = 0.5,
     mutation_max = 0.5,
     cores = 1,
     directed = TRUE,
    method = "DD",
     cause_orientation = "row",
     DD_kind = c(
         "in", "out", "entropy_in", "entropy_out",
```

```
"clustering_coefficient", "page_rank", "communities"
),
DD_weight = 1,
max_norm = FALSE,
verbose = FALSE
)
```

classify

Mechanistic Network Classification

# **Description**

Tests a network against hypothetical generating processes using a comparative network inference.

### Usage

```
classify(
  network,
  directed,
  method = "DD",
  net_kind = "matrix",
  mechanism_kind = "canonical",
 DD_kind = c("in", "out", "entropy_in", "entropy_out", "clustering_coefficient",
    "page_rank", "communities", "motifs_3", "motifs_4", "eq_in", "eq_out",
   "eq_entropy_in", "eq_entropy_out", "eq_clustering_coefficient", "eq_page_rank",
    "eq_communities", "eq_motifs_3", "eq_motifs_4"),
 DD_weight = c(0.0735367966, 0.0739940162, 0.0714523761, 0.0708156931, 0.0601296752,
  0.0448072016, 0.0249793608, 0.0733125084, 0.0697029389, 0.0504358835, 0.0004016029,
  0.0563752664, 0.0561878218, 0.0540490099, 0.0504347104, 0.0558106667, 0.0568270319,
    0.0567474398),
  cause_orientation = "row",
  max_norm = FALSE,
  resolution = 100,
  resolution_min = 0.01,
  resolution_max = 0.99,
  reps = 3,
  processes = c("ER", "PA", "DM", "SW", "NM"),
  test = "empirical",
  best_fit_finder = "systematic",
  power_max = 5,
  connectance_max = 0.5,
  divergence_max = 0.5,
  mutation_max = 0.5,
  null_reps = 50,
  best_fit_kind = "avg",
  best_fit_sd = 0,
```

```
ks_dither = 0,
ks_alternative = "two.sided",
cores = 1,
size_different = FALSE,
null_dist_trim = 1,
verbose = FALSE
)
```

#### **Arguments**

network The network to be classified.

directed Whether the target network is directed. If missing this will be inferred by the

symmetry of the input network.

method This determines the method used to compare networks at the heart of the clas-

sification. Currently "DD" (Degree Distribution) and "align" (the align function which compares networks by the entropy of diffusion on them) are supported.

Future versions will allow user-defined methods. Defaults to "DD".

net\_kind If the network is an adjacency matrix ("matrix") or an edge list ("list"). Defaults

to "matrix".

mechanism\_kind Either "canonical" or "grow" can be used to simulate networks. If "grow" is

used, note that here it will only simulate pure mixtures made of a single mecha-

nism. Defaults to "canonical".

DD\_kind = A vector of network properties to be used to compare networks. Defaults to

"all", which is the average of the in- and out-degrees.

DD\_weight = Weights of each network property in DD\_kind. Defaults to 1, which is equal

weighting for each property.

cause\_orientation

= The orientation of directed adjacency matrices. Defaults to "row".

max\_norm Binary variable indicating if each network property should be normalized so its

max value (if a node-level property) is one. Defaults to FALSE.

resolution Defaults to 100. The first step is to find the version of each process most similar

to the target network. This parameter sets the number of parameter values to search across. Decrease to improve performance, but at the cost of accuracy.

resolution\_min Defaults to 0.01. The minimum parameter value to consider. Zero is not used

because in many processes it results in degenerate systems (e.g. entirely unconnected networks). Currently process agnostic. Future versions will accept a

vector of values, one for each process.

resolution\_max Defaults to 0.99. The maximum parameter value to consider. One is not used be-

cause in many processes it results in degenerate systems (e.g. entirely connected networks). Currently process agnostic. Future versions will accept a vector of

values, one for each process.

reps Defaults to 3. The number of networks to simulate for each parameter. More

replicates increases accuracy by making the estimation of the parameter that

produces networks most similar to the target network less idiosyncratic.

processes

Defaults to c("ER", "PA", "DD", "SW", "NM"). Vector of process abbreviations. Currently only the default five are supported. Future versions will accept user-defined network-generating functions and associated parameters. ER = Erdos-Renyi random. PA = Preferential Attachment. DD = Duplication and Divergence. SW = Small World. NM = Niche Model.

test

Defaults to "empirical". The test used to distinguish the null distribution of comparisons between the network being classified and the networks simulated according to a hypothesized mechanism(s), with a particular best-fitting parameter. "empirical" finds how many simulated networks were on average farther from each other than the network being classified is. "KS" uses a KS test. "WMWU" uses a Wilcoxon-Mann-Whitney-U test.

best\_fit\_finder

Defaults to "systematic". Determines how the best-fitting parameter of each mechanism specified in processes is found. "systematic" tries every parameter value from resolution\_min to resolution\_max with a step size of resolution\_max - resolution\_min / resolution. "optim\_L-BFGS-B" uses the L-BFGS-B optimizer in the optimx package. "optim\_GenSA" uses the GenSA optimizer in the GenSA package.

power\_max

Defaults to 5. The maximum power of attachment in the Preferential Attachment process (PA).

connectance\_max

= Defaults to 0.5. The maximum connectance parameter for the Niche Model.

divergence\_max = Defaults to 0.5. The maximum divergence parameter for the Duplication and Divergence/Mutation mechanisms.

= Defaults to 0.5. The maximum mutation parameter for the Duplication and mutation\_max Mutation mechanism.

> Defaults to 50. The number of best fit networks to simulate that will be used to create a null distribution of distances between networks within the given process, which will then be used to test if the target network appears unusually distant from them and therefore likely not governed by that process.

Defaults to "avg". If null reps is more than 1, the fit of each parameter has to best\_fit\_kind be an aggregate statistic of the fit of all the null reps networks. Must be 'avg', 'median', 'min', or 'max'.

> Defaults to 0. Standard Deviation used to simulate networks with a similar but not identical best fit parameter. This is important because simulating networks with the identical parameter can artificially inflate the false negative rate by assuming the best fit parameter is the true parameter. For large resolution and reps values this will become true, but can be computationally intractable for realistically large systems.

> Defaults to 0. The KS test cannot compute exact p-values when every pairwise network distance is not unique. Adding small amounts of noise makes each distance unique. We are not aware of a study on the impacts this has on accuracy so it is set to zero by default.

ks\_alternative Defaults to "two.sided". Governs the KS test. Assuming best\_fit\_sd is not too large, this can be set to "greater" because the target network cannot be more

null\_reps

best\_fit\_sd

ks\_dither

alike identically simulated networks than they are to each other. In practice we have found "greater" and "less" produce numerical errors. Only "two.sided", "less", and "greater" are supported through stats::ks.test().

Defaults to 1. The number of cores to run the classification on. When set to 1

parallelization will be ignored.

size\_different = If there is a difference in the size of the networks used in the null distribution.

Defaults to FALSE.

null\_dist\_trim = Number between zero and one that determines how much of each network

comparison distribution (unknown network compared to simulated networks, simulated networks compared to each other) should be used. Prevents p-value convergence with large sample sizes. Defaults to 1, which means all compar-

isons are used (no trimming).

verbose Defaults to FALSE. Whether to print all messages.

#### **Details**

cores

Note: Currently each process is assumed to have a single governing parameter.

#### Value

A dataframe with 3 columns and as many rows as processes being tested (5 by default). The first column lists the processes. The second lists the p-value on the null hypothesis that the target network did come from that row's process. The third column gives the estimated parameter for that particular process.

### References

Langendorf, R. E., & Burgess, M. G. (2020). Empirically Classifying Network Mechanisms. arXiv preprint arXiv:2012.15863.

```
# Import netcom
library(netcom)

# Adjacency matrix
size <- 10
network <- matrix(sample(c(0,1), size = size^2, replace = TRUE), nrow = size, ncol = size)

# Classify this network
# This can take several minutes to run
classify(network, processes = c("ER", "PA", "DM", "SW", "NM"))</pre>
```

12 classify\_Systematic

classify\_Systematic Mechanistic Network Classification

**Description** 

Tests a network against hypothetical generating processes using a comparative network inference.

### Usage

```
classify_Systematic(
  network,
  directed = FALSE,
 method = "DD",
  net_kind = "matrix",
 DD_kind = c("in", "out", "entropy_in", "entropy_out", "clustering_coefficient",
    "page_rank", "communities", "motifs_3", "motifs_4", "eq_in", "eq_out",
  "eq_entropy_in", "eq_entropy_out", "eq_clustering_coefficient", "eq_page_rank",
    "eq_communities", "eq_motifs_3", "eq_motifs_4"),
 DD_weight = c(0.0735367966, 0.0739940162, 0.0714523761, 0.0708156931, 0.0601296752,
  0.0448072016, 0.0249793608, 0.0733125084, 0.0697029389, 0.0504358835, 0.0004016029,
  0.0563752664, 0.0561878218, 0.0540490099, 0.0504347104, 0.0558106667, 0.0568270319,
    0.0567474398),
  cause_orientation = "row",
  max_norm = FALSE,
  resolution = 100,
  resolution_min = 0.01,
  resolution_max = 0.99,
  reps = 3,
  processes = c("ER", "PA", "DM", "SW", "NM"),
  power_max = 5,
  connectance_max = 0.5,
  divergence_max = 0.5,
  mutation_max = 0.5,
  null_reps = 50,
  best_fit_kind = "avg",
  best_fit_sd = 0.01,
  ks_dither = 0,
  ks_alternative = "two.sided",
  cores = 1,
  size_different = FALSE,
  null_dist_trim = 1,
  verbose = TRUE
)
```

### **Arguments**

network

The network to be classified.

classify\_Systematic 13

directed Defaults to TRUE. Whether the target network is directed. This determines the method used to compare networks at the heart of the clasmethod sification. Currently "DD" (Degree Distribution) and "align" (the align function which compares networks by the entropy of diffusion on them) are supported. Future versions will allow user-defined methods. Defaults to "DD". net\_kind If the network is an adjacency matrix ("matrix") or an edge list ("list"). Defaults to "matrix". DD\_kind = A vector of network properties to be used to compare networks. Defaults to "all", which is the average of the in- and out-degrees. DD\_weight = Weights of each network property in DD\_kind. Defaults to 1, which is equal weighting for each property. cause\_orientation = The orientation of directed adjacency matrices. Defaults to "row". Binary variable indicating if each network property should be normalized so its max\_norm max value (if a node-level property) is one. Defaults to FALSE. resolution Defaults to 100. The first step is to find the version of each process most similar to the target network. This parameter sets the number of parameter values to search across. Decrease to improve performance, but at the cost of accuracy. resolution\_min Defaults to 0.01. The minimum parameter value to consider. Zero is not used because in many processes it results in degenerate systems (e.g. entirely unconnected networks). Currently process agnostic. Future versions will accept a vector of values, one for each process. Defaults to 0.99. The maximum parameter value to consider. One is not used beresolution\_max cause in many processes it results in degenerate systems (e.g. entirely connected networks). Currently process agnostic. Future versions will accept a vector of values, one for each process. Defaults to 3. The number of networks to simulate for each parameter. More reps replicates increases accuracy by making the estimation of the parameter that produces networks most similar to the target network less idiosyncratic. processes

Defaults to c("ER", "PA", "DD", "SW", "NM"). Vector of process abbrevia-

tions. Currently only the default five are supported. Future versions will accept user-defined network-generating functions and associated parameters. ER = Erdos-Renyi random. PA = Preferential Attachment. DD = Duplication and

Divergence. SW = Small World. NM = Niche Model.

Defaults to 5. The maximum power of attachment in the Preferential Attachment power\_max

process (PA).

connectance\_max

= Defaults to 0.5. The maximum connectance parameter for the Niche Model.

divergence\_max = Defaults to 0.5. The maximum divergence parameter for the Duplication and

Divergence/Mutation mechanisms.

= Defaults to 0.5. The maximum mutation parameter for the Duplication and mutation\_max

Mutation mechanism.

null\_reps Defaults to 50. The number of best fit networks to simulate that will be used to

create a null distribution of distances between networks within the given process,

14 classify\_Systematic

which will then be used to test if the target network appears unusually distant from them and therefore likely not governed by that process.

best\_fit\_kind Defaults to "avg". If null\_reps is more than 1, the fit of each parameter has to

be an aggregate statistic of the fit of all the null\_reps networks. Must be 'avg',

'median', 'min', or 'max'.

best\_fit\_sd Defaults to 0.01. Standard Deviation used to simulate networks with a simi-

lar but not identical best fit parameter. This is important because simulating networks with the identical parameter artificially inflates the false negative rate by assuming the best fit parameter is the true parameter. For large resolution and reps values this will become true, but also computationally intractable for

realistically large systems.

ks\_dither Defaults to 0. The KS test cannot compute exact p-values when every pairwise

network distance is not unique. Adding small amounts of noise makes each distance unique. We are not aware of a study on the impacts this has on accuracy

so it is set to zero by default.

ks\_alternative Defaults to "two.sided". Governs the KS test. Assuming best\_fit\_sd is not too

large, this can be set to "greater" because the target network cannot be more alike identically simulated networks than they are to each other. In practice we have found "greater" and "less" produce numerical errors. Only "two.sided",

"less", and "greater" are supported through stats::ks.test().

cores Defaults to 1. The number of cores to run the classification on. When set to 1

parallelization will be ignored.

size\_different = If there is a difference in the size of the networks used in the null distribution.

Defaults to FALSE.

null\_dist\_trim = Number between zero and one that determines how much of each network

comparison distribution (unknown network compared to simulated networks, simulated networks compared to each other) should be used. Prevents p-value convergence with large sample sizes. Defaults to 1, which means all compar-

isons are used (no trimming).

verbose Defaults to TRUE. Whether to print all messages.

### **Details**

Note: Currently each process is assumed to have a single governing parameter.

#### Value

A dataframe with 3 columns and as many rows as processes being tested (5 by default). The first column lists the processes. The second lists the p-value on the null hypothesis that the target network did come from that row's process. The third column gives the estimated parameter for that particular process.

### References

Langendorf, R. E., & Burgess, M. G. (2020). Empirically Classifying Network Mechanisms. arXiv preprint arXiv:2012.15863.

compare 15

### **Examples**

```
# Import netcom
library(netcom)

# Adjacency matrix
size <- 10
network <- matrix(sample(c(0,1), size = size^2, replace = TRUE), nrow = size, ncol = size)

# Classify this network
# This can take several minutes to run
classify(network, processes = c("ER", "PA", "DM", "SW", "NM"))</pre>
```

compare

Compare Networks Many-to-Many

### **Description**

Compares one network to a list of many networks.

### Usage

```
compare(
  networks,
  net_kind = "matrix",
  method = "DD",
  cause_orientation = "row",
  DD_kind = "all",
  DD_weight = 1,
  max_norm = FALSE,
  size_different = FALSE,
  cores = 1,
  diffusion_sampling = 2,
  diffusion_limit = 10,
  verbose = FALSE
)
```

# **Arguments**

networks The networks being compared to the target network

to "matrix".

method This determines the method used to compare networks at the heart of the clas-

sification. Currently "DD" (Degree Distribution) and "align" (the align function which compares networks by the entropy of diffusion on them) are supported.

Future versions will allow user-defined methods. Defaults to "DD".

16 compare

cause\_orientation

= The orientation of directed adjacency matrices. Defaults to "row".

DD\_kind = A vector of network properties to be used to compare networks. Defaults to

"all", which is the average of the in- and out-degrees.

DD\_weight = Weights of each network property in DD\_kind. Defaults to 1, which is equal

weighting for each property.

max\_norm Binary variable indicating if each network property should be normalized so its

max value (if a node-level property) is one. Defaults to FALSE.

size\_different Defaults to FALSE. If TRUE, will ensure the node-level properties being com-

pared are vectors of the same length, which is accomplished using splines.

cores Defaults to 1. The number of cores to run the classification on. When set to 1

parallelization will be ignored.

diffusion\_sampling

Base of the power to use to nonlinearly sample the diffusion kernels if method

= "align". Defaults to 2.

diffusion\_limit

Number of markov steps in the diffusion kernels if method = "align". Defaults

to 10.

verbose Defaults to TRUE. Whether to print all messages.

#### **Details**

Note: Currently each process is assumed to have a single governing parameter.

### Value

A square matrix with dimensions equal to the number of networks being compared, where the ij element is the comparison of networks i and j.

#### References

Langendorf, R. E., & Burgess, M. G. (2020). Empirically Classifying Network Mechanisms. arXiv preprint arXiv:2012.15863.

compare\_Target 17

```
replace = TRUE),
nrow = size,
ncol = size)
}
compare(networks = networks)
```

compare\_Target

Compare Networks One-to-Many

# Description

Compares one network to a list of many networks.

The network be compared.

### Usage

```
compare_Target(
  target,
  networks,
  net_size,
  net_kind = "matrix",
  method = "DD",
  cause_orientation = "row",
  DD_kind = "all",
  DD_weight = 1,
  max_norm = FALSE,
  cores = 1,
  verbose = FALSE
)
```

### **Arguments**

target

networks

The networks being compared to the target network

Size

net\_kind

If the network is an adjacency matrix ("matrix") or an edge list ("list"). Defaults to "matrix".

method

This determines the method used to compare networks at the heart of the classification. Currently "DD" (Degree Distribution) and "align" (the align function which compares networks by the entropy of diffusion on them) are supported. Future versions will allow user-defined methods. Defaults to "DD".

cause\_orientation

= The orientation of directed adjacency matrices. Defaults to "row".

DD\_kind = A vector of network properties to be used to compare networks. Defaults to

"all", which is the average of the in- and out-degrees.

18 compare\_Target

DD_weight	= Weights of each network property in DD_kind. Defaults to 1, which is equal weighting for each property.
max_norm	Binary variable indicating if each network property should be normalized so its max value (if a node-level property) is one. Defaults to FALSE.
cores	Defaults to 1. The number of cores to run the classification on. When set to 1 parallelization will be ignored.
verbose	Defaults to TRUE. Whether to print all messages.

### **Details**

Note: Currently each process is assumed to have a single governing parameter.

### Value

A pseudo-distance vector where the i-element is the comparison between the target network and the ith network being compared to.

### References

Langendorf, R. E., & Burgess, M. G. (2020). Empirically Classifying Network Mechanisms. arXiv preprint arXiv:2012.15863.

```
# Import netcom
library(netcom)
# Adjacency matrix
size <- 10
comparisons <- 50
network\_target \leftarrow matrix(sample(c(0,1), size = size^2, replace = TRUE), nrow = size, ncol = size)
network_others <- list()</pre>
for (net in 1:comparisons) {
     network_others[[net]] = matrix(
         sample(
             c(0,1),
             size = size^2,
             replace = TRUE),
         nrow = size,
         ncol = size)
}
compare_Target(target = network_target, networks = network_others, net_size = size, method = "DD")
```

gini 19

gini Gini coefficient

### Description

Takes a matrix and returns the Gini coefficient of each column.

### Usage

```
gini(input, byrow = FALSE)
```

# **Arguments**

input A matrix where the Gini coefficient will be calculated on each column. Note

that vector data must be converted to a single-column matrix.

byrow Defaults to FALSE. Set to TRUE to calculate the Gini coefficient of each row.

### Value

A vector of the Gini coefficients of each column.

### References

Gini, C. (1912). Variabilita e mutabilita. Reprinted in Memorie di metodologica statistica (Ed. Pizetti E, Salvemini, T). Rome: Libreria Eredi Virgilio Veschi.

# **Examples**

```
# Vectors are not supported. First convert to a single-column matrix.
sample_data <- runif(20, 0, 1)
gini(matrix(sample_data, ncol = 1))

# Multiple Gini coefficients can be calculated simultaneously
gini(matrix(sample_data, ncol = 2))</pre>
```

grow\_DD

Grow a Duplication and Divergence Network

# Description

Grows an already existing network by adding a node according to the Duplication and Divergence mechanism. Nodes can only attach to previously grown nodes.

20 grow\_DD

### Usage

```
grow_DD(
  matrix,
  x,
  divergence,
  link = 0,
  connected = FALSE,
  retcon = FALSE,
  directed = TRUE
)
```

#### **Arguments**

matrix Existing network to experience growth.

x The ID of the node to be grown.

divergence Probability that the new node loses edges associated with the node it duplicates.

Needs to be between zero and one.

link Probability that the new node attaches to the node it duplicates. Defaults to 0.

connected Binary argument determining if the newly grown node has to be connected to the

existing network. Defaults to FALSE, to prevent rare computational slow-downs

when it is unlikely to create a connected network. Defaults to FALSE.

retcon Binary variable determining if already existing nodes can attach to new nodes.

Defaults to FALSE.

directed Binary variable determining if the network is directed, resulting in off-diagonal

asymmetry in the adjacency matrix. Defaults to TRUE.

### **Details**

Different from Duplication & Mutation models in that edges can only be lost.

### Value

An adjacency matrix.

#### References

Ispolatov, I., Krapivsky, P. L., & Yuryev, A. (2005). Duplication-divergence model of protein interaction network. Physical review E, 71(6), 061911.

```
# Import netcom
library(netcom)

size <- 10
existing_network <- matrix(sample(c(0,1), size = size^2, replace = TRUE), nrow = size, ncol = size)
new_network_prep <- matrix(0, nrow = size + 1, ncol = size + 1)
new_network_prep[1:size, 1:size] = existing_network</pre>
```

grow\_DM 21

```
new_network <- grow_DD(matrix = new_network_prep, x = size + 1, divergence = 0.5)</pre>
```

grow\_DM

Grow a Duplication and Mutation Network

# **Description**

Grows an already existing network by adding a node according to the Duplication and Mutation mechanism. Nodes can only attach to previously grown nodes.

# Usage

```
grow_DM(
  matrix,
  x,
  divergence,
  mutation = 0,
  link = 0,
  connected = FALSE,
  retcon = FALSE,
  directed = TRUE
)
```

### **Arguments**

matrix	Existing network to experience growth.
X	The ID of the node to be grown.
divergence	Probability that the new node loses edges associated with the node it duplicates. Needs to be between zero and one.
mutation	Probability that the new node gains edges not associated with the node it duplicates. Needs to be between zero and one.
link	Probability that the new node attaches to the node it duplicates. Defaults to 0.
connected	Binary argument determining if the newly grown node has to be connected to the existing network. Defaults to FALSE, to prevent rare computational slow-downs when it is unlikely to create a connected network. Defaults to FALSE.
retcon	Binary variable determining if already existing nodes can attach to new nodes. Defaults to FALSE.
directed	Binary variable determining if the network is directed, resulting in off-diagonal asymmetry in the adjacency matrix. Defaults to TRUE.

# **Details**

Different from Duplication & Mutation models in that edges can only be lost.

22 grow\_ER

#### Value

An adjacency matrix.

#### References

Ispolatov, I., Krapivsky, P. L., & Yuryev, A. (2005). Duplication-divergence model of protein interaction network. Physical review E, 71(6), 061911.

### **Examples**

```
# Import netcom
library(netcom)

size <- 10
existing_network <- matrix(sample(c(0,1), size = size^2, replace = TRUE), nrow = size, ncol = size)
new_network_prep <- matrix(0, nrow = size + 1, ncol = size + 1)
new_network_prep[1:size, 1:size] = existing_network
new_network <- grow_DM(matrix = new_network_prep, x = size + 1, divergence = 0.5)</pre>
```

grow\_ER

Grow an Erdos-Renyi Random Network

### **Description**

Grows an already existing network by adding a node according to the Erdos-Renyi random mechanism. Nodes can only attach to previously grown nodes.

# Usage

```
grow_ER(matrix, x, p, retcon = FALSE, directed = TRUE)
```

# Arguments

matrix Existing network to experience growth.

x The ID of the node to be grown.

p Probability possible edges exist. Needs to be between zero and one.

retcon Binary variable determining if already existing nodes can attach to new nodes. Defaults to FALSE.

directed Binary variable determining if the network is directed, resulting in off-diagonal asymmetry in the adjacency matrix. Defaults to TRUE.

#### Details

Different from Duplication & Mutation models in that edges can only be lost.

grow\_NM 23

# Value

An adjacency matrix.

### References

Erdos, P. and Renyi, A., On random graphs, Publicationes Mathematicae 6, 290–297 (1959).

# **Examples**

```
# Import netcom
library(netcom)

size <- 10
existing_network <- matrix(sample(c(0,1), size = size^2, replace = TRUE), nrow = size, ncol = size)
new_network_prep <- matrix(0, nrow = size + 1, ncol = size + 1)
new_network_prep[1:size, 1:size] = existing_network
new_network <- grow_ER(matrix = new_network_prep, x = size + 1, p = 0.5)</pre>
```

grow\_NM

Grow a Niche Model Network

# **Description**

Grows an already existing network by adding a node according to the Niche Model mechanism. Nodes can only attach to previously grown nodes.

### Usage

```
grow_NM(matrix, x, niches, connectance = 0.2, directed = TRUE, retcon = FALSE)
```

# **Arguments**

matrix	Existing network to experience growth.
X	The ID of the node to be grown.
niches	Vector of length x, with values between zero and one corresponding to each node's niche.
connectance	Niche Model parameter specifying the expected connectivity of the network, which determines for a given node the niche space window within which it attaches to every other node. Defaults to 0.2.
directed	Binary variable determining if the network is directed, resulting in off-diagonal asymmetry in the adjacency matrix. Defaults to TRUE.
retcon	Binary variable determining if already existing nodes can attach to new nodes. Defaults to FALSE.

grow\_PA

### **Details**

Stirs a node in a Niche Model network.

### Value

An adjacency matrix.

# References

Williams, R. J., & Martinez, N. D. (2000). Simple rules yield complex food webs. Nature, 404(6774), 180-183.

# Examples

```
# Import netcom
library(netcom)

size <- 10
existing_network <- matrix(sample(c(0,1), size = size^2, replace = TRUE), nrow = size, ncol = size)
new_network_prep <- matrix(0, nrow = size + 1, ncol = size + 1)
new_network_prep[1:size, 1:size] = existing_network
new_network <- grow_NM(matrix = new_network_prep, x = size + 1, niches = stats::runif(size))</pre>
```

grow\_PA

Grow a Preferential Attachment Network

# Description

Grows an already existing network by adding a node according to the Preferential Attachment mechanism. Nodes can only attach to previously grown nodes.

# Usage

```
grow_PA(
  matrix,
  x,
  power,
  sum_v_max = "sum",
  nascent_help = TRUE,
  retcon = FALSE,
  directed = TRUE
)
```

grow\_PA 25

# **Arguments**

matrix	Existing network to experience growth.
X	The ID of the node to be grown.
power	Power of attachment, which determines how much new nodes prefer to attach to nodes that have many edges compared to few. Needs to be positive.
sum_v_max	Degree distributions must be normalized, either by their "max" or "sum". Defaults to "max".
nascent_help	Should a single edge be added to the degree distribution of all nodes so that nodes with a zero in-degree can still have a chance of being attached to by new nodes. Defaults to TRUE.
retcon	Binary variable determining if already existing nodes can attach to new nodes. Defaults to FALSE.
directed	Binary variable determining if the network is directed, resulting in off-diagonal asymmetry in the adjacency matrix. Defaults to TRUE.

#### **Details**

Adds a node in a network according to the Preferential Attachment mechanism.

### Value

An adjacency matrix.

# References

Barabási, A. L., & Albert, R. (1999). Emergence of scaling in random networks. science, 286(5439), 509-512.

```
# Import netcom
library(netcom)

size <- 10
existing_network <- matrix(sample(c(0,1), size = size^2, replace = TRUE), nrow = size, ncol = size)
new_network_prep <- matrix(0, nrow = size + 1, ncol = size + 1)
new_network_prep[1:size, 1:size] = existing_network
new_network <- grow_PA(matrix = new_network_prep, x = size + 1, power = 2.15)</pre>
```

26 grow\_SW

grow_SW	Grow a Small-World Network	
---------	----------------------------	--

### **Description**

Grows an already existing network by adding a node according to the Small-World mechanism. Nodes can only attach to previously grown nodes.

# Usage

```
grow_SW(matrix, x, rewire, connected = FALSE, retcon = FALSE, directed = TRUE)
```

# Arguments

matrix	Existing network to experience growth.
x	The ID of the node to be grown.
rewire	Small-World parameter specifying the probability each edge is randomly rewired, allowing for the possiblity of bridges between connected communities.
connected	Binary argument determining if the newly grown node has to be connected to the existing network. Defaults to FALSE, to prevent rare computational slow-downs when it is unlikely to create a connected network. Defaults to False.
retcon	Binary variable determining if already existing nodes can attach to new nodes. Defaults to FALSE.
directed	Binary variable determining if the network is directed, resulting in off-diagonal asymmetry in the adjacency matrix. Defaults to TRUE.

# **Details**

Grows a node in a network according to the Small-World mechanism.

#### Value

An adjacency matrix.

# References

Watts, D. J., & Strogatz, S. H. (1998). Collective dynamics of 'small-world' networks. nature, 393(6684), 440-442.

```
# Import netcom
library(netcom)

size <- 10
existing_network <- matrix(sample(c(0,1), size = size^2, replace = TRUE), nrow = size, ncol = size)
new_network_prep <- matrix(0, nrow = size + 1, ncol = size + 1)</pre>
```

ics 27

```
new_network_prep[1:size, 1:size] = existing_network
new_network <- grow_SW(matrix = new_network_prep, x = size + 1, rewire = 0.213)</pre>
```

ics

Induced Conserved Structure (ICS)

# Description

Calculates the Induced Conserved Structure proposed by Patro and Kingsford (2012) of an alignment between two networks.

### Usage

```
ics(network_1_input, network_2_input, alignment, flip = FALSE)
```

### Arguments

network\_1\_input

The first network being aligned, which must be in matrix form. If the two networks are of different sizes, it will be easier to interpret the output if this is the smaller one.

network\_2\_input

The second network, which also must be a matrix.

alignment A matrix, such as is output by the function NetCom, where the first two columns

contain corresponding node IDs for the two networks that were aligned.

contain corresponding node 1Ds for the two networks that were anglied.

flip Defaults to FALSE. Set to TRUE if the first network is larger than the second. This is necessary because ICS is not a symmetric measure of alignment quality.

### Value

A number ranging between 0 and 1. If the Induced Conserved Structure is 1, the two networks are isomorphic (identical) under the given alignment.

#### References

Patro, R., & Kingsford, C. (2012). Global network alignment using multiscale spectral signatures. Bioinformatics, 28(23), 3105-3114.

```
# Note that ICS is only defined on unweighted networks.
net_one <- round(matrix(runif(25,0,1), nrow=5, ncol=5))
net_two <- round(matrix(runif(25,0,1), nrow=5, ncol=5))
ics(net_two, net_two, align(net_one, net_two)$alignment)</pre>
```

28 make\_DD

make_DD	Makes a Duplication and Divergence Network	

# **Description**

Makes a network according to the Duplication and Divergence mechanism.

# Usage

```
make_DD(size, net_kind, divergence, directed = TRUE)
```

# **Arguments**

size Number of nodes in the network.

net\_kind If the network is an adjacency matrix ("matrix") or an edge list ("list").

divergence Probability that the new node loses edges associated with the node it duplicates.

Needs to be between zero and one.

directed Whether the target network is directed. Defaults to TRUE.

#### **Details**

Different from Duplication & Mutation models in that edges can only be lost.

### Value

An adjacency matrix.

#### References

Ispolatov, I., Krapivsky, P. L., & Yuryev, A. (2005). Duplication-divergence model of protein interaction network. Physical review E, 71(6), 061911.

```
# Import netcom
library(netcom)

# Network size (number of nodes)
size <- 10

# Divergence parameter
divergence <- 0.237

# Make network according to the Duplication & Divergence mechanism
make_DD(size = size, net_kind = "matrix", divergence = divergence)</pre>
```

make\_DM 29

make_DM	Make a Duplication and Mutation Network

# **Description**

Make an already existing network according to the Duplication and Mutation mechanism.

# Usage

```
make_DM(size, net_kind, divergence, mutation, directed = FALSE)
```

# Arguments

size	Number of nodes in the network.
net_kind	If the network is an adjacency matrix ("matrix") or an edge list ("list").
divergence	Probability that the new node loses edges associated with the node it duplicates. Needs to be between zero and one.
mutation	Probability that the new node gains edges not associated with the node it duplicates. Needs to be between zero and one.
directed	Binary variable determining if the network is directed, resulting in off-diagonal asymmetry in the adjacency matrix. Defaults to TRUE.

# **Details**

Different from Duplication & Mutation models in that edges can only be lost.

# Value

An adjacency matrix.

# References

Ispolatov, I., Krapivsky, P. L., & Yuryev, A. (2005). Duplication-divergence model of protein interaction network. Physical review E, 71(6), 061911.

```
# Import netcom
library(netcom)

# Network size (number of nodes)
size <- 10

# Divergence parameter
divergence <- 0.237

# Mutation parameter</pre>
```

30 make\_Mixture

```
mutation <- 0.1
# Make network according to the Duplication & Mutation mechanism
make_DM(size = size, net_kind = "matrix", divergence = divergence, mutation = mutation)</pre>
```

make\_Mixture

Make a Mixture Mechanism Network

### **Description**

Creates a network by iteratively adding or rewiring nodes, each capable of attaching to existing nodes according to a user-specified mechanism.

# Usage

```
make_Mixture(
  mechanism,
  directed,
  parameter,
  kind,
  size,
  niches,
  retcon = FALSE,
  link_DD = 0,
  link_DM = 0,
  force_connected = FALSE)
```

### **Arguments**

mechanism

A vector of mechanism names corresponding to the mechanisms each node acts in accordance with. Note that the first two mechanisms are irrelevant because the first two nodes default to connecting to each other. Currently supported mechanisms: "ER" (Erdos-Renyi random), "PA", (Preferential Attachment), "DD", (Duplication and Divergence), "DM" (Duplication and Mutation), "SW", (Small-World), and "NM" (Niche Model).

directed

A binary variable determining if the network is directed, resulting in off-diagonal asymmetry in the adjacency matrix. Either a single value or a vector of values the same length as the mechanism input vector.

parameter

Parameter of each node's mechanism. Either a single value or a vector of values the same length as the mechanism input vector.

kind

Either 'grow' or 'rewire', and determines if the nodes specified in the mechanism input vector are to be rewired or grown. Either a single value or a vector of values the same length as the mechanism input vector. The number of 'grow' nodes, excluding the first two which are always a pair of bidirectionally connected nodes, is the size of the final network.

31 make\_Mixture

size	Typically not specified. The size of the network depends on how many 'grow' events are part of the 'kind' input sequence. This should only be used when all four components of the network evolution ('mechanism', 'kind', 'parameter', and 'directed') are single name inputs instead of vectors.
niches	Used by the Niche Model to determine which nodes interact. Needs to be a vector of the same length as the number of nodes, and range between zero and one.
retcon	Binary variable determining if already existing nodes can attach to new nodes. Defaults to FALSE.
link_DD	Defaults to 0. A second parameter in the DD (Duplication & Divergence). Currently only one parameter per mechanism can be specified.
link_DM	Defaults to 0. A second parameter in the DM (Duplication & Mutation). Currently only one parameter per mechanism can be specified.
force connected	

force\_connected

Defaults to FALSE. Determines if nodes can be added to the growing network that are disconnected. If TRUE, this is prevented by re-determining the offending node's edges until the network is connected.

#### **Details**

This function grows, one node at a time, a mixture mechanism network. As each node is added to the growing network it can attach to existing nodes by its own node-specific mechanism. A sequence of mechanism names must be provided. Note: Currently each mechanism is assumed to have a single governing parameter.

### Value

An unweighted mixture mechanism adjacency matrix.

### References

Langendorf, R. E., & Burgess, M. G. (2020). Empirically Classifying Network Mechanisms. arXiv preprint arXiv:2012.15863.

```
# Import netcom
library(netcom)
# Start by creating a sequence of network evolutions.
# There are four components to this sequence that can each be defined for every step
# in the network's evolution. Or, you can also specify a component once which will
# be used for every step in the newtwork's evolution.
mechanism <- c(</pre>
   rep("ER", 7),
   rep("PA", 2),
    rep("ER", 3)
)
```

32 make\_NM

```
kind <- c(
    rep("grow", 7),
    rep("rewire", 2),
    rep("grow", 3)
)
parameter <- c(
    rep(0.3, 7),
    rep(2, 2),
    rep(0.3, 3)
)
directed <- c(</pre>
    rep(TRUE, 7),
    rep(FALSE, 2),
    rep(TRUE, 3)
)
# Simulate a network according to the rules of this system evolution.
network <- make_Mixture(</pre>
     mechanism = mechanism,
     kind = kind,
     parameter = parameter,
     directed = directed
)
```

make\_NM

Make a Niche Model network

# Description

Creates a single network according to the Niche Model. Can be directed or undirected, but is always unweighted.

# Usage

```
make_NM(
    size,
    niches,
    net_kind = "matrix",
    connectance = 0.1,
    directed = TRUE,
    grow = FALSE
)
```

### **Arguments**

size

The number of nodes in the network. Must be a positive integer.

make\_Null 33

niches	A vector of numbers specifying the niche of each member of the system (node). Each niche value must be element of [0,1].
net_kind	The format of the network. Currently must be either 'matrix' or 'list'.
connectance	Defaults to 0.5. The ratio of actual interactions to possible interactions. Effects the beta distributed width of niche values each member of the system (node) interacts with.
directed	If FALSE all interactions will be made symmetric. Note that the process of creating interactions is unaffected by this choice. Defaults to TRUE.
grow	Binary argument that determines if the network should be made in a growing fashion, where nodes' edges are added in order of their niches and can only attach to previously considered nodes. Defaults to FALSE.

# Value

An interaction matrix format of a Niche Model network.

# References

Williams, R. J., & Martinez, N. D. (2000). Simple rules yield complex food webs. Nature, 404(6774), 180-183.

# **Examples**

```
# Import netcom
library(netcom)

# Network size (number of nodes)
size <- 10

# Create niche values for each member of the system (node)
niches <- stats::runif(n = size)

# Make network according to the Niche Model
make_NM(size = size, niches = niches)</pre>
```

make\_Null

Mechanism Null Distributions

# Description

Creates a null distribution for a mechanism and parameter combination.

34 make\_Null

### Usage

```
make_Null(
  input_network,
  net_kind,
 mechanism_kind,
 process,
  parameter,
  net_size,
  iters,
 method,
  neighborhood,
 DD_kind,
 DD_weight,
  directed,
  resolution_min = 0.01,
  resolution_max = 0.99,
  power_max = 5,
  connectance_max = 0.5,
  divergence_max = 0.5,
  best_fit_sd = 0,
  cores = 1,
  size_different = FALSE,
  cause_orientation = "row",
 max_norm = FALSE,
  verbose = FALSE
)
```

### Arguments

input\_network The network for which to create a null distribution.

net\_kind If the network is an adjacency matrix ("matrix") or an edge list ("list"). Defaults

to "matrix".

mechanism\_kind Either "canonical" or "grow" can be used to simulate networks. If "grow" is

used, note that here it will only simulate pure mixtures made of a single mecha-

nism.

process Name of mechanism. Currently only "ER", "PA", "DD", "DM" "SW", and

"NM" are supported. Future versions will accept user-defined network-generating functions and associated parameters. ER = Erdos-Renyi random. PA = Preferential Attachment. DD = Duplication and Divergence. DM = Duplication and

Mutation. SW = Small World. NM = Niche Model.

parameter Parameter in the governing mechanism.

net\_size Number of nodes in the network.

iters Number of replicates in the null distribution. Note that length(null\_dist) =

((iters^2)-iters)/2.

method This determines the method used to compare networks at the heart of the clas-

sification. Currently "DD" (Degree Distribution) and "align" (the align function

make\_Null 35

which compares networks by the entropy of diffusion on them) are supported. Future versions will allow user-defined methods.

neighborhood The range of nodes that form connected communities. Note: This implementa-

tion results in overlap of communities.

DD\_kind = A vector of network properties to be used to compare networks.

DD\_weight = A vector of weights for the relative importance of the network properties

in DD\_kind being used to compare networks. Should be the same length as

DD kind.

directed Whether the target network is directed.

resolution\_min The minimum parameter value to consider. Zero is not used because in many

processes it results in degenerate systems (e.g. entirely unconnected networks). Currently process agnostic. Future versions will accept a vector of values, one

for each process. Defaults to 0.01.

resolution\_max The maximum parameter value to consider. One is not used because in many

processes it results in degenerate systems (e.g. entirely connected networks). Currently process agnostic. Future versions will accept a vector of values, one

for each process. Defaults to 0.99.

power\_max Defaults to 5. The maximum power of attachment in the Preferential Attachment

process (PA).

connectance\_max

Defaults to 0.5. The maximum connectance parameter for the Niche Model.

divergence\_max Defaults to 0.5. The maximum divergence parameter for the Duplication and

Divergence/Mutation mechanisms.

best\_fit\_sd Defaults to 0.01. Standard Deviation used to simulate networks with a simi-

lar but not identical best fit parameter. This is important because simulating networks with the identical parameter artificially inflates the false negative rate by assuming the best fit parameter is the true parameter. For large resolution and reps values this will become true, but also computationally intractable for

realistically large systems.

cores Defaults to 1. The number of cores to run the classification on. When set to 1

parallelization will be ignored.

size\_different If there is a difference in the size of the networks used in the null distribution.

Defaults to FALSE.

cause\_orientation

The orientation of directed adjacency matrices. Defaults to "row".

max\_norm Binary variable indicating if each network property should be normalized so its

max value (if a node-level property) is one. Defaults to FALSE.

verbose Defaults to FALSE. Whether to print all messages.

#### **Details**

Produces ground-truthing network data.

### Value

A list. The first element contains the networks. The second contains their corresponding parameters.

36 make\_Null\_canonical

### References

Langendorf, R. E., & Burgess, M. G. (2020). Empirically Classifying Network Mechanisms. arXiv preprint arXiv:2012.15863.

# **Examples**

```
# Import netcom
library(netcom)
make_Systematic(net_size = 10)
```

make\_Null\_canonical

Mechanism Null Distributions

# Description

Creates a null distribution for a mechanism and parameter combination.

### Usage

```
make_Null_canonical(
  input_network,
  net_kind,
  process,
  parameter,
  net_size,
  iters,
 method,
 neighborhood,
 DD_kind,
 DD_weight,
  directed,
  resolution_min = 0.01,
  resolution_max = 0.99,
  power_max = 5,
  connectance_max = 0.5,
  divergence_max = 0.5,
  best_fit_sd = 0,
  cores = 1,
  size_different = FALSE,
  cause_orientation = "row",
 max_norm = FALSE,
  verbose = FALSE
)
```

make\_Null\_canonical 37

#### **Arguments**

input\_network The network for which to create a null distribution.

net\_kind If the network is an adjacency matrix ("matrix") or an edge list ("list"). Defaults

to "matrix".

process Name of mechanism. Currently only "ER", "PA", "DD", "DM" "SW", and

"NM" are supported. Future versions will accept user-defined network-generating functions and associated parameters. ER = Erdos-Renyi random. PA = Preferential Attachment. DD = Duplication and Divergence. DM = Duplication and

Mutation. SW = Small World. NM = Niche Model.

parameter Parameter in the governing mechanism.

net\_size Number of nodes in the network.

iters Number of replicates in the null distribution. Note that length(null\_dist) =

((iters^2)-iters)/2.

method This determines the method used to compare networks at the heart of the clas-

sification. Currently "DD" (Degree Distribution) and "align" (the align function which compares networks by the entropy of diffusion on them) are supported.

Future versions will allow user-defined methods.

neighborhood The range of nodes that form connected communities. Note: This implementa-

tion results in overlap of communities.

DD\_kind A vector of network properties to be used to compare networks.

DD\_weight A vector of weights for the relative importance of the network properties in

DD\_kind being used to compare networks. Should be the same length as DD\_kind.

directed Whether the target network is directed.

resolution\_min The minimum parameter value to consider. Zero is not used because in many

processes it results in degenerate systems (e.g. entirely unconnected networks). Currently process agnostic. Future versions will accept a vector of values, one

for each process. Defaults to 0.01.

resolution\_max The maximum parameter value to consider. One is not used because in many

processes it results in degenerate systems (e.g. entirely connected networks). Currently process agnostic. Future versions will accept a vector of values, one

for each process. Defaults to 0.99.

power\_max Defaults to 5. The maximum power of attachment in the Preferential Attachment

process (PA).

connectance\_max

Defaults to 0.5. The maximum connectance parameter for the Niche Model.

divergence\_max Defaults to 0.5. The maximum divergence parameter for the Duplication and

Divergence/Mutation mechanisms.

best\_fit\_sd Defaults to 0.01. Standard Deviation used to simulate networks with a simi-

lar but not identical best fit parameter. This is important because simulating networks with the identical parameter artificially inflates the false negative rate by assuming the best fit parameter is the true parameter. For large resolution and reps values this will become true, but also computationally intractable for

realistically large systems.

38 make\_Null\_mixture

cores Defaults to 1. The number of cores to run the classification on. When set to 1

parallelization will be ignored.

size\_different If there is a difference in the size of the networks used in the null distribution.

Defaults to FALSE.

cause\_orientation

The orientation of directed adjacency matrices. Defaults to "row".

max\_norm Binary variable indicating if each network property should be normalized so its

max value (if a node-level property) is one. Defaults to FALSE.

verbose Defaults to FALSE. Whether to print all messages.

#### **Details**

Produces ground-truthing network data.

# Value

A list. The first element contains the networks. The second contains their corresponding parameters.

#### References

Langendorf, R. E., & Burgess, M. G. (2020). Empirically Classifying Network Mechanisms. arXiv preprint arXiv:2012.15863.

# **Examples**

```
# Import netcom
library(netcom)
make_Systematic(net_size = 10)
```

make\_Null\_mixture

Mechanism Null Distributions

## **Description**

Creates a null distribution for a mechanism and parameter combination.

# Usage

```
make_Null_mixture(
  input_network,
  net_kind,
  process,
  parameter,
  net_size,
  iters,
```

make\_Null\_mixture 39

```
method,
 neighborhood,
 DD_kind,
 DD_weight,
 directed,
  resolution_min = 0.01,
  resolution_max = 0.99,
  power_max = 5,
  connectance_max = 0.5,
  divergence_max = 0.5,
 best_fit_sd = 0,
  cores = 1,
  size_different = FALSE,
  cause_orientation = "row",
 max_norm = FALSE,
  verbose = FALSE
)
```

#### **Arguments**

input\_network The network for which to create a null distribution.

net\_kind If the network is an adjacency matrix ("matrix") or an edge list ("list"). Defaults

to "matrix".

process Name of mechanism. Currently only "ER", "PA", "DD", "DM" "SW", and

"NM" are supported. Future versions will accept user-defined network-generating functions and associated parameters. ER = Erdos-Renyi random. PA = Preferential Attachment. DD = Duplication and Divergence. DM = Duplication and

Mutation. SW = Small World. NM = Niche Model.

parameter Parameter in the governing mechanism.

net\_size Number of nodes in the network.

iters Number of replicates in the null distribution. Note that length(null dist) =

((iters^2)-iters)/2.

method This determines the method used to compare networks at the heart of the clas-

sification. Currently "DD" (Degree Distribution) and "align" (the align function which compares networks by the entropy of diffusion on them) are supported.

Future versions will allow user-defined methods.

neighborhood The range of nodes that form connected communities. Note: This implementa-

tion results in overlap of communities.

DD\_kind A vector of network properties to be used to compare networks.

DD\_weight A vector of weights for the relative importance of the network properties in

DD\_kind being used to compare networks. Should be the same length as DD\_kind.

directed Whether the target network is directed.

resolution\_min The minimum parameter value to consider. Zero is not used because in many

processes it results in degenerate systems (e.g. entirely unconnected networks). Currently process agnostic. Future versions will accept a vector of values, one

for each process. Defaults to 0.01.

40 make\_Null\_mixture

resolution\_max The maximum parameter value to consider. One is not used because in many processes it results in degenerate systems (e.g. entirely connected networks). Currently process agnostic. Future versions will accept a vector of values, one

for each process. Defaults to 0.99.

power\_max Defaults to 5. The maximum power of attachment in the Preferential Attachment

process (PA).

connectance\_max

Defaults to 0.5. The maximum connectance parameter for the Niche Model.

divergence\_max Defaults to 0.5. The maximum divergence parameter for the Duplication and

Divergence/Mutation mechanisms.

best\_fit\_sd Defaults to 0.01. Standard Deviation used to simulate networks with a simi-

lar but not identical best fit parameter. This is important because simulating networks with the identical parameter artificially inflates the false negative rate by assuming the best fit parameter is the true parameter. For large resolution and reps values this will become true, but also computationally intractable for

realistically large systems.

cores Defaults to 1. The number of cores to run the classification on. When set to 1

parallelization will be ignored.

size\_different If there is a difference in the size of the networks used in the null distribution.

Defaults to FALSE.

cause\_orientation

The orientation of directed adjacency matrices. Defaults to "row".

max\_norm Binary variable indicating if each network property should be normalized so its

max value (if a node-level property) is one. Defaults to FALSE.

verbose Defaults to FALSE. Whether to print all messages.

# **Details**

Produces ground-truthing network data.

#### Value

A list. The first element contains the networks. The second contains their corresponding parameters.

#### References

Langendorf, R. E., & Burgess, M. G. (2020). Empirically Classifying Network Mechanisms. arXiv preprint arXiv:2012.15863.

#### **Examples**

```
# Import netcom
library(netcom)
```

make\_Systematic(net\_size = 10)

make\_SW 41

make_SW Makes a Small-World Network
-------------------------------------

# **Description**

Make an already existing network according to the Small-World mechanism.

# Usage

```
make_SW(size, rewire, neighborhood, net_kind = "matrix", directed = FALSE)
```

# **Arguments**

size	The number of nodes in the network. Must be a positive integer.
rewire	Small-World parameter specifying the probability each edge is randomly rewired, allowing for the possibility of bridges between connected communities.
neighborhood	The range of nodes that form connected communities. Note: This implementation results in overlap of communities.
net_kind	The format of the network. Currently must be either 'matrix' or 'list'.x
directed	Binary variable determining if the network is directed, resulting in off-diagonal asymmetry in the adjacency matrix. Defaults to TRUE.

#### **Details**

Rewires a node in a network according to the Small-World mechanism.

#### Value

An adjacency matrix.

#### References

Watts, D. J., & Strogatz, S. H. (1998). Collective dynamics of 'small-world'networks. nature, 393(6684), 440-442.

```
# Import netcom
library(netcom)

# Network size (number of nodes)
size <- 10

# Rewiring parameter
rewire <- 0.2

# Make network according to the Small-World mechanism
make_SW(size = size, net_kind = "matrix", rewire = rewire)</pre>
```

42 make\_Systematic

make\_Systematic

Systematically Make Networks

# Description

Creates a list of networks that systematically spans mechanisms and their respective parameters.

# Usage

```
make_Systematic(
 net_size,
 neighborhood,
 directed = TRUE,
 net_kind = "matrix",
 mechanism_kind = "canonical",
  resolution = 100,
  resolution_min = 0.01,
  resolution_max = 0.99,
  reps = 3,
  processes = c("ER", "PA", "DM", "SW", "NM"),
 power_max = 5,
  connectance_max = 0.5,
  divergence_max = 0.5,
 mutation_max = 0.5,
 canonical = FALSE,
  cores = 1,
  verbose = TRUE
)
```

# **Arguments**

net_size	Number of nodes in the network.
neighborhood	The range of nodes that form connected communities. Note: This implementation results in overlap of communities.
directed	Whether the target network is directed. Defaults to TRUE.
net_kind	If the network is an adjacency matrix ("matrix") or an edge list ("list"). Defaults to "matrix".
mechanism_kind	Either "canonical" or "grow" can be used to simulate networks. If "grow" is used, note that here it will only simulate pure mixtures made of a single mechanism. Defaults to "canonical".
resolution	The first step is to find the version of each process most similar to the target network. This parameter sets the number of parameter values to search across. Decrease to improve performance, but at the cost of accuracy. Defaults to 100.

make\_Systematic 43

resolution_min	= The minimum parameter value to consider. Zero is not used because in many processes it results in degenerate systems (e.g. entirely unconnected networks). Currently process agnostic. Future versions will accept a vector of values, one for each process. Defaults to 0.01.
resolution_max	The maximum parameter value to consider. One is not used because in many processes it results in degenerate systems (e.g. entirely connected networks). Currently process agnostic. Future versions will accept a vector of values, one for each process. Defaults to 0.99.
reps	Defaults to 3. The number of networks to simulate for each parameter. More replicates increases accuracy by making the estimation of the parameter that produces networks most similar to the target network less idiosyncratic.
processes	Defaults to c("ER", "PA", "DD", "SW", "NM"). Vector of process abbreviations. Currently only the default five are supported. Future versions will accept user-defined network-generating functions and associated parameters. ER = Erdos-Renyi random. PA = Preferential Attachment. DD = Duplication and Divergence. SW = Small World. NM = Niche Model.
power_max	Defaults to 5. The maximum power of attachment in the Preferential Attachment process (PA).
connectance_max	
	Defaults to 0.5. The maximum connectance parameter for the Niche Model.
divergence_max	Defaults to 0.5. The maximum divergence parameter for the Duplication and Divergence/Mutation mechanisms.
mutation_max	Defaults to $0.5$ . The maximum mutation parameter for the Duplication and Mutation mechanism.
canonical	Defautls to FALSE. If TRUE the mechanisms are directed or undirected in accordance with their canonical forms. This negates the value of 'directed'.
cores	Defaults to 1. The number of cores to run the classification on. When set to 1 parallelization will be ignored.

# Details

verbose

Produces ground-truthing network data.

# Value

A list. The first element contains the networks. The second contains their corresponding parameters.

Defaults to TRUE. Whether to print all messages.

# References

Langendorf, R. E., & Burgess, M. G. (2020). Empirically Classifying Network Mechanisms. arXiv preprint arXiv:2012.15863.

# **Examples**

```
# Import netcom
library(netcom)

make_Systematic(net_size = 10)
```

make\_Systematic\_canonical

Systematically Make Networks

# **Description**

Creates a list of networks that systematically spans mechanisms and their respective parameters.

# Usage

```
make_Systematic_canonical(
  net_size,
  neighborhood,
 directed = TRUE,
  net_kind = "matrix",
  resolution = 100,
  resolution_min = 0.01,
  resolution_max = 0.99,
  reps = 3,
  processes = c("ER", "PA", "DM", "SW", "NM"),
  power_max = 5,
  connectance_max = 0.5,
  divergence_max = 0.5,
 mutation_max = 0.5,
  cores = 1,
  verbose = TRUE
)
```

# **Arguments**

net_size	Number of nodes in the network.
neighborhood	The range of nodes that form connected communities. Note: This implementation results in overlap of communities.
directed	Whether the target network is directed. Defaults to TRUE.
net_kind	If the network is an adjacency matrix ("matrix") or an edge list ("list"). Defaults to "matrix".
resolution	The first step is to find the version of each process most similar to the target network. This parameter sets the number of parameter values to search across. Decrease to improve performance, but at the cost of accuracy. Defaults to 100.

resolution\_min = The minimum parameter value to consider. Zero is not used because in many

processes it results in degenerate systems (e.g. entirely unconnected networks). Currently process agnostic. Future versions will accept a vector of values, one

for each process. Defaults to 0.01.

resolution\_max The maximum parameter value to consider. One is not used because in many

processes it results in degenerate systems (e.g. entirely connected networks). Currently process agnostic. Future versions will accept a vector of values, one

for each process. Defaults to 0.99.

reps Defaults to 3. The number of networks to simulate for each parameter. More

replicates increases accuracy by making the estimation of the parameter that

produces networks most similar to the target network less idiosyncratic.

processes Defaults to c("ER", "PA", "DD", "SW", "NM"). Vector of process abbrevia-

tions. Currently only the default five are supported. Future versions will accept user-defined network-generating functions and associated parameters. ER = Erdos-Renyi random. PA = Preferential Attachment. DD = Duplication and

Divergence. SW = Small World. NM = Niche Model.

power\_max = Defaults to 5. The maximum power of attachment in the Preferential Attach-

ment process (PA).

connectance\_max

= Defaults to 0.5. The maximum connectance parameter for the Niche Model.

divergence\_max = Defaults to 0.5. The maximum divergence parameter for the Duplication and

Divergence/Mutation mechanisms.

mutation\_max = Defaults to 0.5. The maximum mutation parameter for the Duplication and

Mutation mechanism.

cores = Defaults to 1. The number of cores to run the classification on. When set to 1

parallelization will be ignored.

verbose = Defaults to TRUE. Whether to print all messages.

#### Details

Produces ground-truthing network data.

#### Value

A list. The first element contains the networks. The second contains their corresponding parameters.

#### References

Langendorf, R. E., & Burgess, M. G. (2020). Empirically Classifying Network Mechanisms. arXiv preprint arXiv:2012.15863.

```
# Import netcom
library(netcom)
make_Systematic(net_size = 10)
```

```
\begin{tabular}{ll} make\_Systematic\_directedCanonicalLike \\ Systematically\ Make\ Networks \\ \end{tabular}
```

# **Description**

Creates a list of networks that systematically spans mechanisms and their respective parameters.

# Usage

```
make_Systematic_directedCanonicalLike(
  net_size,
 directed = TRUE,
  net_kind = "matrix",
  resolution = 100,
  resolution_min = 0.01,
  resolution_max = 0.99,
  reps = 3,
  processes = c("ER", "PA", "DM", "SW", "NM"),
  power_max = 5,
  connectance_max = 0.5,
  divergence_max = 0.5,
 mutation_max = 0.5,
  cores = 1,
  verbose = TRUE
)
```

# Arguments

net_size	Number of nodes in the network.
directed	Whether the target network is directed. Defaults to TRUE.
net_kind	If the network is an adjacency matrix ("matrix") or an edge list ("list"). Defaults to "matrix".
resolution	The first step is to find the version of each process most similar to the target network. This parameter sets the number of parameter values to search across. Decrease to improve performance, but at the cost of accuracy. Defaults to 100.
resolution_min	= The minimum parameter value to consider. Zero is not used because in many processes it results in degenerate systems (e.g. entirely unconnected networks). Currently process agnostic. Future versions will accept a vector of values, one for each process. Defaults to 0.01.
resolution_max	The maximum parameter value to consider. One is not used because in many processes it results in degenerate systems (e.g. entirely connected networks). Currently process agnostic. Future versions will accept a vector of values, one

for each process. Defaults to 0.99.

reps	Defaults to 3. The number of networks to simulate for each parameter. More replicates increases accuracy by making the estimation of the parameter that produces networks most similar to the target network less idiosyncratic.
processes	Defaults to c("ER", "PA", "DD", "SW", "NM"). Vector of process abbreviations. Currently only the default five are supported. Future versions will accept user-defined network-generating functions and associated parameters. ER = Erdos-Renyi random. PA = Preferential Attachment. DD = Duplication and Divergence. SW = Small World. NM = Niche Model.
power_max	= Defaults to 5. The maximum power of attachment in the Preferential Attachment process (PA).
connectance_max	X
	= Defaults to 0.5. The maximum connectance parameter for the Niche Model.
divergence_max	= Defaults to 0.5. The maximum divergence parameter for the Duplication and Divergence/Mutation mechanisms.
mutation_max	= Defaults to 0.5. The maximum mutation parameter for the Duplication and Mutation mechanism.
cores	= Defaults to 1. The number of cores to run the classification on. When set to 1 parallelization will be ignored.

# **Details**

verbose

Produces ground-truthing network data.

#### Value

A list. The first element contains the networks. The second contains their corresponding parameters.

= Defaults to TRUE. Whether to print all messages.

# References

Langendorf, R. E., & Burgess, M. G. (2020). Empirically Classifying Network Mechanisms. arXiv preprint arXiv:2012.15863.

```
# Import netcom
library(netcom)

make_Systematic(net_size = 10)
```

```
make_Systematic_mixture
```

Systematically Make Networks

# **Description**

Creates a list of networks that systematically spans mechanisms and their respective parameters.

# Usage

```
make_Systematic_mixture(
 net_size,
 neighborhood,
 directed = TRUE,
  net_kind = "matrix",
  resolution = 100,
  resolution_min = 0.01,
  resolution_{max} = 0.99,
  reps = 3,
  processes = c("ER", "PA", "DM", "SW", "NM"),
  power_max = 5,
  connectance_max = 0.5,
  divergence_max = 0.5,
 mutation_max = 0.5,
 canonical = FALSE,
  cores = 1,
  verbose = TRUE
)
```

# Arguments

net_size	Number of nodes in the network.
neighborhood	The range of nodes that form connected communities. Note: This implementation results in overlap of communities.
directed	Whether the target network is directed. Defaults to TRUE.
net_kind	If the network is an adjacency matrix ("matrix") or an edge list ("list"). Defaults to "matrix".
resolution	The first step is to find the version of each process most similar to the target network. This parameter sets the number of parameter values to search across. Decrease to improve performance, but at the cost of accuracy. Defaults to 100.
resolution_min	= The minimum parameter value to consider. Zero is not used because in many processes it results in degenerate systems (e.g. entirely unconnected networks). Currently process agnostic. Future versions will accept a vector of values, one for each process. Defaults to 0.01.

resolution_max	The maximum parameter value to consider. One is not used because in many processes it results in degenerate systems (e.g. entirely connected networks). Currently process agnostic. Future versions will accept a vector of values, one for each process. Defaults to 0.99.
reps	Defaults to 3. The number of networks to simulate for each parameter. More replicates increases accuracy by making the estimation of the parameter that produces networks most similar to the target network less idiosyncratic.
processes	Defaults to c("ER", "PA", "DD", "SW", "NM"). Vector of process abbreviations. Currently only the default five are supported. Future versions will accept user-defined network-generating functions and associated parameters. ER = Erdos-Renyi random. PA = Preferential Attachment. DD = Duplication and Divergence. SW = Small World. NM = Niche Model.
power_max	Defaults to 5. The maximum power of attachment in the Preferential Attachment process (PA).
connectance_max	X
	Defaults to 0.5. The maximum connectance parameter for the Niche Model.
divergence_max	Defaults to 0.5. The maximum divergence parameter for the Duplication and Divergence/Mutation mechanisms.
mutation_max	Defaults to 0.5. The maximum mutation parameter for the Duplication and Mutation mechanism.
canonical	Defautls to FALSE. If TRUE the mechanisms are directed or undirected in accordance with their canonical forms. This negates the value of 'directed'.
cores	= Defaults to 1. The number of cores to run the classification on. When set to 1 parallelization will be ignored.

# **Details**

verbose

Produces ground-truthing network data.

# Value

A list. The first element contains the networks. The second contains their corresponding parameters.

= Defaults to TRUE. Whether to print all messages.

## References

Langendorf, R. E., & Burgess, M. G. (2020). Empirically Classifying Network Mechanisms. arXiv preprint arXiv:2012.15863.

```
# Import netcom
library(netcom)

make_Systematic(net_size = 10)
```

50 null\_fit\_optim

null\_fit\_optim

Empirical parameterization via null distributions

# Description

Helper function to find the best fitting version of a mechanism by searching across the null distributions associated with a process + parameter combination.

#### Usage

```
null_fit_optim(
  parameter,
  process,
  network,
  net_size,
  iters,
  neighborhood,
  directed,
  DD_kind,
  DD_weight,
  net_kind,
 mechanism_kind,
 method,
  size_different,
  power_max,
  connectance_max,
  divergence_max,
  best_fit_sd,
  max_norm,
  cause_orientation,
  cores,
  null_dist_trim,
  ks_dither,
  ks_alternative,
  verbose = FALSE
)
```

# Arguments

parameter

The parameter being tested for its ability to generate networks alike the input 'network'.

process

Name of mechanism. Currently only "ER", "PA", "DD", "DM" "SW", and "NM" are supported. Future versions will accept user-defined network-generating functions and associated parameters. ER = Erdos-Renyi random. PA = Preferential Attachment. DD = Duplication and Divergence. DM = Duplication and Mutation. SW = Small World. NM = Niche Model.

50

null\_fit\_optim 51

network The network being compared to a hypothesized 'process' with a given 'parame-

ter' value.

net\_size Number of nodes in the network.

iters Number of replicates in the null distribution. Note that length(null\_dist) =

((iters^2)-iters)/2.

neighborhood The range of nodes that form connected communities. Note: This implementa-

tion results in overlap of communities.

directed Whether the target network is directed.

DD\_kind A vector of network properties to be used to compare networks.

DD\_weight A vector of weights for the relative importance of the network properties in

DD\_kind being used to compare networks. Should be the same length as DD\_kind.

net\_kind If the network is an adjacency matrix ("matrix") or an edge list ("list").

mechanism\_kind Either "canonical" or "grow" can be used to simulate networks. If "grow" is

used, note that here it will only simulate pure mixtures made of a single mecha-

nism.

method This determines the method used to compare networks at the heart of the clas-

sification. Currently "DD" (Degree Distribution) and "align" (the align function which compares networks by the entropy of diffusion on them) are supported.

Future versions will allow user-defined methods.

size\_different If there is a difference in the size of the networks used in the null distribution.

power\_max The maximum power of attachment in the Preferential Attachment process (PA).

connectance\_max

The maximum connectance parameter for the Niche Model.

divergence\_max The maximum divergence parameter for the Duplication and Divergence/Mutation

mechanisms.

best\_fit\_sd Standard Deviation used to simulate networks with a similar but not identical

best fit parameter. This is important because simulating networks with the identical parameter artificially inflates the false negative rate by assuming the best fit parameter is the true parameter. For large resolution and reps values this will become true, but also computationally intractable for realistically large systems.

max\_norm Binary variable indicating if each network property should be normalized so its

max value (if a node-level property) is one.

cause\_orientation

The orientation of directed adjacency matrices.

cores The number of cores to run the classification on. When set to 1 parallelization

will be ignored.

null\_dist\_trim = Number between zero and one that determines how much of each network

comparison distribution (unknown network compared to simulated networks, simulated networks compared to each other) should be used. Prevents p-value convergence with large sample sizes. Defaults to 1, which means all compar-

isons are used (no trimming).

ks\_dither The KS test cannot compute exact p-values when every pairwise network dis-

tance is not unique. Adding small amounts of noise makes each distance unique. We are not aware of a study on the impacts this has on accuracy so it is set to

zero by default.

52 null\_fit\_optim

ks\_alternative Governs the KS test. Assuming best\_fit\_sd is not too large, this can be set to "greater" because the target network cannot be more alike identically simulated networks than they are to each other. In practice we have found "greater" and "less" produce numerical errors. Only "two.sided", "less", and "greater" are supported through stats::ks.test().

verbose

Defaults to TRUE. Whether to print all messages.

#### **Details**

Note: Currently each process is assumed to have a single governing parameter.

#### Value

A number measuring how different the input network is from the parameter + process combination.

#### References

Langendorf, R. E., & Burgess, M. G. (2020). Empirically Classifying Network Mechanisms. arXiv preprint arXiv:2012.15863.

```
# Import netcom
library(netcom)
# Adjacency matrix
size <- 10
network <- matrix(sample(c(0,1), size = size^2, replace = TRUE), nrow = size, ncol = size)
# Calculate how similar the input network is to Small-World networks with
# a rewiring probability of 0.28.
null_fit_optim(
     parameter = 0.28,
     process = "SW",
    network = network,
    net\_size = 12,
    iters = 20,
    neighborhood = max(1, round(0.1 * net_size)),
    net_kind = "matrix",
    mechanism_kind = "grow",
    power_max = 5,
     connectance_max = 0.5,
     divergence_max = 0.5,
     cores = 1,
     directed = TRUE,
     method = "DD",
     size_different = FALSE,
     cause_orientation = "row",
    DD_kind = c(
         "in", "out", "entropy_in", "entropy_out",
         "clustering_coefficient", "page_rank", "communities"
     ),
```

stir\_DD 53

```
DD_weight = 1,
best_fit_sd = 0,
max_norm = FALSE,
null_dist_trim = 0,
ks_dither = 0,
ks_alternative = "two.sided",
verbose = FALSE
)
```

stir\_DD

Sitrs a Duplication and Divergence Network

#### **Description**

Stirs an already existing network by rewiring a node according to the Duplication and Divergence mechanism.

# Usage

```
stir_DD(
  matrix,
  x,
  divergence,
  directed = TRUE,
  link = 0,
  force_connected = FALSE
)
```

# **Arguments**

matrix Existing network to be rewired (stirred).

x The ID of the node to be grown.

divergence Probability that the new node loses edges associated with the node it duplicates.

Needs to be between zero and one.

directed Binary variable determining if the network is directed, resulting in off-diagonal

asymmetry in the adjacency matrix.

link Probability that the new node attaches to the node it duplicates. Defaults to 0.

force\_connected

Binary argument determining if the newly grown node has to be connected to the existing network. Defaults to FALSE, to prevent rare computational slow-downs when it is unlikely to create a connected network. Defaults to FALSE.

#### **Details**

Different from Duplication & Mutation models in that edges can only be lost.

54 stir\_DM

#### Value

An adjacency matrix.

#### References

Ispolatov, I., Krapivsky, P. L., & Yuryev, A. (2005). Duplication-divergence model of protein interaction network. Physical review E, 71(6), 061911.

#### **Examples**

```
# Import netcom
library(netcom)

size <- 10
existing_network <- matrix(sample(c(0,1), size = size^2, replace = TRUE), nrow = size, ncol = size)
new_network_prep <- matrix(0, nrow = size + 1, ncol = size + 1)
new_network_prep[1:size, 1:size] = existing_network
new_network <- stir_DD(matrix = new_network_prep, x = size + 1, divergence = 0.5)</pre>
```

stir\_DM

Stirs a Duplication and Mutation Network

# **Description**

Stirs an already existing network by rewiring a node according to the Duplication and Mutation mechanism.

# Usage

```
stir_DM(
  matrix,
  x,
  divergence,
  mutation,
  directed = TRUE,
  link = 0,
  force_connected = FALSE
)
```

#### **Arguments**

matrix Existing network to experience growth.

x The ID of the node to be rewired (stirred).

divergence Probability that the new node loses edges associated with the node it duplicates.

Needs to be between zero and one.

stir\_ER 55

mutation Probability that the new node gains edges not associated with the node it dupli-

cates. Needs to be between zero and one.

directed Binary variable determining if the network is directed, resulting in off-diagonal

asymmetry in the adjacency matrix.

link Probability that the new node attaches to the node it duplicates. Defaults to 0.

force\_connected

Binary argument determining if the newly grown node has to be connected to the existing network. Defaults to FALSE, to prevent rare computational slow-downs when it is unlikely to create a connected network. Defaults to FALSE.

#### **Details**

Different from Duplication & Mutation models in that edges can only be lost.

#### Value

An adjacency matrix.

#### References

Ispolatov, I., Krapivsky, P. L., & Yuryev, A. (2005). Duplication-divergence model of protein interaction network. Physical review E, 71(6), 061911.

#### **Examples**

```
# Import netcom
library(netcom)

size <- 10
existing_network <- matrix(sample(c(0,1), size = size^2, replace = TRUE), nrow = size, ncol = size)
new_network_prep <- matrix(0, nrow = size + 1, ncol = size + 1)
new_network_prep[1:size, 1:size] = existing_network
new_network <- stir_DM(matrix = new_network_prep, x = size + 1, divergence = 0.5, mutation = 0.21)</pre>
```

stir\_ER

Stir an Erdos-Renyi Random Network

## **Description**

Stirs an already existing network by rewiring a node according to the Erdos-Renyi random mechanism.

# Usage

```
stir_ER(matrix, x, p, directed = TRUE, retcon = FALSE)
```

stir\_NM

## **Arguments**

matrix	Existing network to experience growth.
X	The ID of the node to be rewired (stirred).
р	Probability possible edges exist. Needs to be between zero and one.
directed	Binary variable determining if the network is directed, resulting in off-diagonal asymmetry in the adjacency matrix.
retcon	Binary variable determining if already existing nodes can attach to new nodes. Defaults to FALSE.

# **Details**

Different from Duplication & Mutation models in that edges can only be lost.

#### Value

An adjacency matrix.

# References

Erdos, P. and Renyi, A., On random graphs, Publicationes Mathematicae 6, 290–297 (1959).

# **Examples**

```
# Import netcom
library(netcom)

size <- 10
existing_network <- matrix(sample(c(0,1), size = size^2, replace = TRUE), nrow = size, ncol = size)
new_network_prep <- matrix(0, nrow = size + 1, ncol = size + 1)
new_network_prep[1:size, 1:size] = existing_network
new_network <- stir_ER(matrix = new_network_prep, x = size + 1, p = 0.5)</pre>
```

stir\_NM

Stirs a Niche Model Network

# **Description**

Stirs an already existing network by rewiring a node according to the Niche Model mechanism.

# Usage

```
stir_NM(matrix, x, niches, directed = TRUE, connectance = 0.2)
```

stir\_NM 57

## **Arguments**

matrix	Existing network to experience rewiring (stirring).
X	The ID of the node to be grown.
niches	Vector of length x, with values between zero and one corresponding to each node's niche.
directed	Binary variable determining if the network is directed, resulting in off-diagonal asymmetry in the adjacency matrix. Defaults to TRUE.
connectance	Niche Model parameter specifying the expected connectivity of the network, which determines for a given node the niche space window within which it attaches to every other node. Defaults to 0.2.

#### **Details**

Stirs a node in a Niche Model network.

# Value

An adjacency matrix.

#### References

Williams, R. J., & Martinez, N. D. (2000). Simple rules yield complex food webs. Nature, 404(6774), 180-183.

```
# Import netcom
library(netcom)

size <- 10
existing_network <- matrix(sample(c(0,1), size = size^2, replace = TRUE), nrow = size, ncol = size)
new_network_prep <- matrix(0, nrow = size + 1, ncol = size + 1)
new_network_prep[1:size, 1:size] = existing_network
new_network <- stir_NM(
    matrix = new_network_prep,
    x = size + 1,
    connectance = 0.1,
    niches = runif(size + 1)
)</pre>
```

58 stir\_PA

stir\_PA

Stirs a Preferential Attachment Network

# Description

Stirs an already existing network by rewiring a node according to the Preferential Attachment mechanism.

# Usage

```
stir_PA(
  matrix,
  x,
  power,
  directed = TRUE,
  retcon = FALSE,
  sum_v_max = "max",
  nascent_help = TRUE
)
```

# Arguments

matrix	Existing network to experience growth.
X	The ID of the node to be rewired (stirred).
power	Power of attachment, which determines how much new nodes prefer to attach to nodes that have many edges compared to few. Needs to be positive.
directed	Binary variable determining if the network is directed, resulting in off-diagonal asymmetry in the adjacency matrix.
retcon	Binary variable determining if already existing nodes can attach to new nodes. Defaults to FALSE.
sum_v_max	Degree distributions must be normalized, either by their "max" or "sum". Defaults to "max".
nascent_help	Should a single edge be added to the degree distribution of all nodes so that nodes with a zero in-degree can still have a chance of being attached to by new nodes. Defaults to TRUE.

# **Details**

Rewires a node in a network according to the Preferential Attachment mechanism.

#### Value

An adjacency matrix.

stir\_SW 59

#### References

Barabási, A. L., & Albert, R. (1999). Emergence of scaling in random networks. science, 286(5439), 509-512.

#### **Examples**

```
# Import netcom
library(netcom)

size <- 10
existing_network <- matrix(sample(c(0,1), size = size^2, replace = TRUE), nrow = size, ncol = size)
new_network_prep <- matrix(0, nrow = size + 1, ncol = size + 1)
new_network_prep[1:size, 1:size] = existing_network
new_network <- stir_PA(matrix = new_network_prep, x = size + 1, power = 2.15)</pre>
```

stir\_SW

Stirs a Small-World Network

#### **Description**

Stirs an already existing network by rewiring a node according to the Small-World mechanism.

#### Usage

```
stir_SW(matrix, x, rewire, directed = TRUE)
```

# **Arguments**

matrix Existing network to experience growth.

x The ID of the node to be grown.

rewire Small-World parameter specifying the probability each edge is randomly rewired,

allowing for the possiblity of bridges between connected communities.

directed Binary variable determining if the network is directed, resulting in off-diagonal

asymmetry in the adjacency matrix.

# **Details**

Rewires a node in a network according to the Small-World mechanism.

#### Value

An adjacency matrix.

#### References

Watts, D. J., & Strogatz, S. H. (1998). Collective dynamics of 'small-world'networks. nature, 393(6684), 440-442.

stir\_SW

```
# Import netcom
library(netcom)

size <- 10
existing_network <- matrix(sample(c(0,1), size = size^2, replace = TRUE), nrow = size, ncol = size)
new_network_prep <- matrix(0, nrow = size + 1, ncol = size + 1)
new_network_prep[1:size, 1:size] = existing_network
new_network <- stir_SW(matrix = new_network_prep, x = size + 1, rewire = 0.213)</pre>
```

# **Index**

```
align, 2
best_fit_optim, 5
classify, 8
classify_Systematic, 12
compare, 15
compare_Target, 17
gini, 19
grow_DD, 19
grow_DM, 21
grow_ER, 22
grow_NM, 23
grow_PA, 24
grow_SW, 26
ics, 27
make\_DD, 28
make_DM, 29
make_Mixture, 30
make_NM, 32
make_Null, 33
{\tt make\_Null\_canonical}, 36
make_Null_mixture, 38
make_SW, 41
{\tt make\_Systematic}, \textcolor{red}{42}
make_Systematic_canonical, 44
{\tt make\_Systematic\_directedCanonicalLike},
         46
make_Systematic_mixture, 48
null_fit_optim, 50
stir_DD, 53
stir_DM, 54
stir_ER, 55
stir_NM, 56
stir_PA, 58
stir_SW, 59
```